

Find the area under the curve $y = \sin(x)$ for $0 \le x \le \pi$ using the Trapezoid Rule Exact answer: $\int_{0}^{\pi} (\sin x) dx = -\cos x \Big|_{0}^{\pi} = 2.0$

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Don't do it this way ! $\begin{array}{ll} \mbox{const double A} = 0.; \\ \mbox{const double B} = M_PI; \\ \mbox{double dx} = (B-A)/(float) (\mbox{numSubdivisions} -1); \\ \mbox{double sum} = (\mbox{ Function}(A) + \mbox{Function}(B) \mbox{) }/2.; \\ \mbox{double sum} = (\mbox{ Function}(A) + \mbox{ Function}(B) \mbox{) }/2.; \\ \mbox{double sum} = (\mbox{ Function}(A) + \mbox{ Function}(B) \mbox{) }/2.; \\ \mbox{double sum} = (\mbox{ Function}(A) + \mbox{ Function}(B) \mbox{) }/2.; \\ \mbox{double sum} = (\mbox{ Function}(A) + \mbox{ Function}(B) \mbox{) }/2.; \\ \mbox{double sum} = (\mbox{ Function}(A) + \mbox{ Function}(B) \mbox{) }/2.; \\ \mbox{double sum} = (\mbox{ Function}(A) + \mbox{ Function}(B) \mbox{) }/2.; \\ \mbox{double sum} = (\mbox{ Function}(A) + \mbox{ Function}(B) \mbox{) }/2.; \\ \mbox{double sum} = (\mbox{ Function}(A) + \mbox{ Function}(B) \mbox{) }/2.; \\ \mbox{double sum} = (\mbox{ Function}(A) + \mbox{ Function}(B) \mbox{) }/2.; \\ \mbox{double sum} = (\mbox{ Function}(A) + \mbox{ Function}(B) \mbox{) }/2.; \\ \mbox{double sum} = (\mbox{ Function}(A) + \mbox{ Function}(B) \mbox{) }/2.; \\ \mbox{double sum} = (\mbox{ Function}(A) + \mbox{ Function}(B) \mbox{) }/2.; \\ \mbox{double sum} = (\mbox{ Function}(A) + \mbox{ Function}(B) \mbox{) }/2.; \\ \mbox{double sum} = (\mbox{ Function}(A) + \mbox{ Function}(B) \mbox{) }/2.; \\ \mbox{ }/2.; \\ \mbox{$ omp_set_num_threads(numThreads); #pragma omp parallel for default(none), shared(dx,sum) for(int i = 1; i < numSubdivisions - 1; i++) double x = A + dx * (float) i; double f = Function(x); sum += f; There is no guarantee when each thread will execute this line There is not even a guarantee that each thread will finish this line before some other thread interrupts it. Assembly code: Load sum What if the scheduler decides to switch threads right here? Add f University Computer Graphics Store sum

The answer should be 2.0 exactly, but in 30 trials, it's not even close.4 And, the answers aren't even consistent. How do we fix this? 0.469635 0.398893 0.446419 0.431204 0.517984 0.438868 0.437553 0.501783 0.334996 0.398761 0.506564 0.484124 0.489211 0.584810 0.506362 0.448226 0.434737 0.476670 0.444919 0.442432 0.548837 0.530668 0.500062 0.672593 0.411158 0.363092 0.408718 0.356299 0.523448

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The answer should be 2.0 exactly, but in 30 trials, it's not even close.5 And, the answers aren't even consistent. How do we fix this? Trial #

There are Three Ways to Make the Summing Work Correctly: #1: Atomic 1 #pragma omp parallel for shared(dx) for(int i = 0; i < numSubdivisions; i++) double x = A + dx * (float) i; double f = Function(x); #pragma omp atomic sum += f; More lightweight than *critical* (#2)
Uses a hardware instruction CMPXCHG (compare-and-exchange) · Can only handle these operations: x++, ++x, x--, --x x op= expr , x = x op expr , x = expr op x where op is one of: +, -, *, /, &, |, ^, <<, >>

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There are Three Ways to Make the Summing Work Correctly:

#2: Critical

#pragma omp parallel for shared(dx)
for(int i = 0; i < numSubdivisions; i++)
{
    double x = A + dx * (float) i;
    double f = Function(x);
    #pragma omp critical
    sum += f;
}

• More heavyweight than atomic (#1)
• Allows only one thread at a time to enter this block of code (similar to a mutex)
• Can have any operations you want in this block of code
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Speed of Reduction vs. Atomic vs. Critical

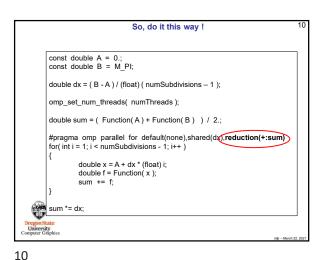
(up = faster)

Reduction

Atomic

Critical

1 2 3



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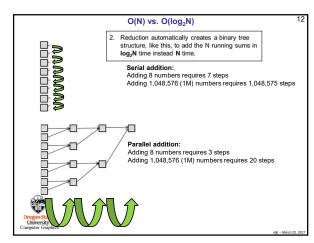
Two Reasons Why Reduction is so Much Better in this Case

#pragma omp parallel for shared(dx),reduction(+:sum)
for(int i = 0; i < numSubdivisions; i++)
{
 double x = A + dx * (float) i;
 double f = Function(x);
 sum += f;
}

1. Reduction secretly creates a temporary private variable for each thread's running sum. Each thread adding into its own running sum, and so threads don't need to slow down to get out of the way of each other.

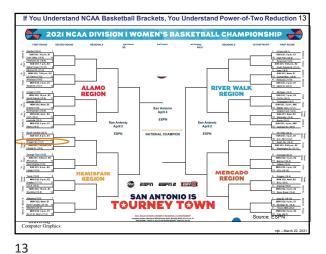
2. Reduction automatically creates a binary tree structure, like this, to add the N running sums in log₂N time instead N time.

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Why Not Do Reduction by Creating Your Own sums Array,
                                       one for each Thread, Like This?
  \label{eq:float} \begin{split} &\text{float *sums = new float [ omp_get_num_threads() ];} \\ &\text{for( int i = 0; i < omp_get_num_threads(); i++)} \\ &\text{sums[ i ] = 0.;} \end{split}
  #pragma omp parallel for private(myPartialSum),shared(sums) for( int i = 0; i < N; i++ )  
         myPartialSum = ...
          sums[ omp_get_thread_num() ] += myPartialSum;
 float sum = 0.;
for( int i= 0; i < omp_get_num_threads( ); i++ )
sum += sums[ i ];
 delete [] sums;
 • This seems perfectly reasonable, it works, and it gets rid of the problem of multiple threads trying to write into the same reduction variable.
\bullet The reason we don't do this is that this method provokes a problem called _{\rm C} \, False Sharing. We will get to that when we discuss caching.
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