## **OpenMP Reduction Case Study: Trapezoid Integration Example**

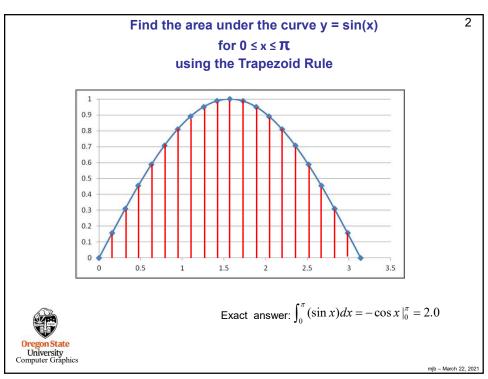




tranezoid notx

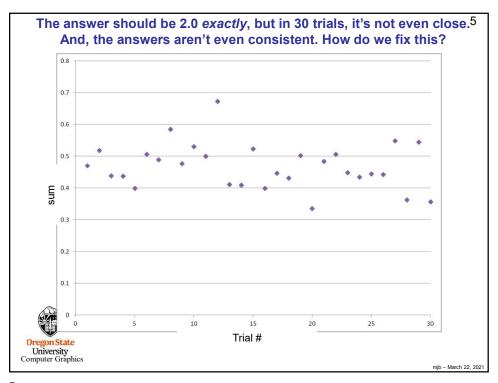
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1



```
3
                                       Don't do it this way!
   const double A = 0.;
   const double B = M PI;
   double dx = (B - A)/(float) (numSubdivisions - 1);
   double sum = ( Function( A ) + Function( B ) ) / 2.;
   omp_set_num_threads( numThreads );
   #pragma omp parallel for default(none), shared(dx,sum)
   for(int i = 1; i < numSubdivisions - 1; i++)
              double x = A + dx * (float) i;
              double f = Function(x);
              sum += f; ≼
   sum *= dx;
  · There is no guarantee when each thread will execute this line
    There is not even a guarantee that each thread will finish this line
     before some other thread interrupts it.
                            Assembly code:
                                                              What if the scheduler decides to
                            Load sum
                                                              switch threads right here?
                            Add f
                            Store sum
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```
The answer should be 2.0 exactly, but in 30 trials, it's not even close.4
      And, the answers aren't even consistent. How do we fix this?
                         0.469635
                                          0.398893
                         0.517984
                                          0.446419
                         0.438868
                                          0.431204
                                          0.501783
                         0.437553
                                          0.334996
                         0.398761
                                          0.484124
                         0.506564
                                          0.506362
                         0.489211
                                          0.448226
                         0.584810
                                          0.434737
                         0.476670
                         0.530668
                                          0.444919
                         0.500062
                                          0.442432
                         0.672593
                                          0.548837
                         0.411158
                                          0.363092
                                          0.544778
                         0.408718
                         0.523448
                                          0.356299
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```



```
There are Three Ways to Make the Summing Work Correctly:
                                    #1: Atomic
   1
       #pragma omp parallel for shared(dx)
       for( int i = 0; i < numSubdivisions; i++)
            double x = A + dx * (float) i;
            double f = Function(x);
            #pragma omp atomic
            sum += f;
         More lightweight than critical (#2)
         Uses a hardware instruction CMPXCHG (compare-and-exchange)
         Can only handle these operations:
              X++, ++X, X--, --X
              x op= expr, x = x op expr, x = expr op x
              where op is one of: +, -, *, /, &, |, ^, <<, >>
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## There are Three Ways to Make the Summing Work Correctly: #2: Critical

2

```
#pragma omp parallel for shared(dx)
for( int i = 0; i < numSubdivisions; i++ )
{
    double x = A + dx * (float) i;
    double f = Function(x);
    #pragma omp critical
    sum += f;
}</pre>
```

- More heavyweight than atomic (#1)
- Allows only one thread at a time to enter this block of code (similar to a mutex)
- · Can have any operations you want in this block of code



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## There are Three Ways to Make the Summing Work Correctly: #3: Reduction

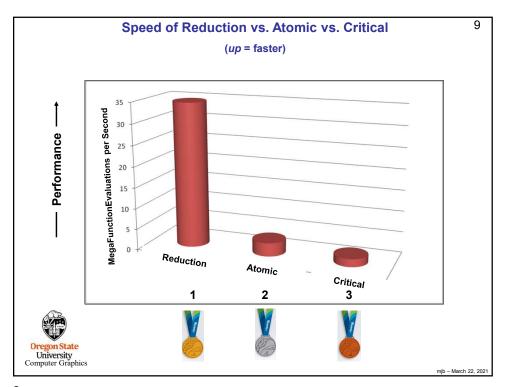
3

```
#pragma omp parallel for shared(dx).reduction(+:sum)
for( int i = 0; i < numSubdivisions; i++ )
{
    double x = A + dx * (float) i;
    double f = Function( x );
    sum += f;
}</pre>
```

- · OpenMP creates code to make this as fast as possible
- Reduction operators can be: + , , \* , & , | , ^ , && , || , max , min

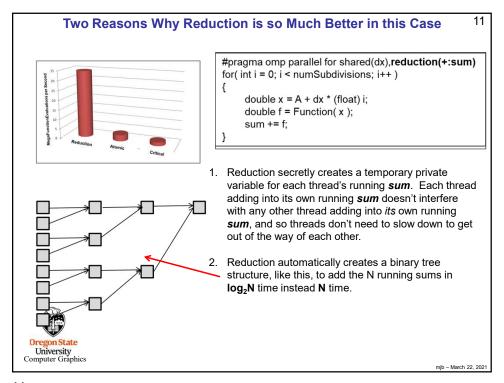


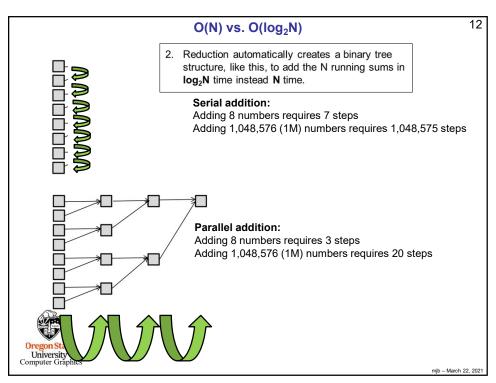
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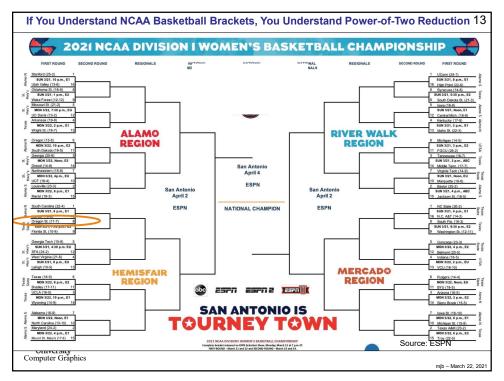


```
Const double A = 0.;
const double B = M_PI;
double dx = (B-A) / (float) (numSubdivisions – 1);
omp_set_num_threads(numThreads);
double sum = (Function(A) + Function(B)) / 2.;
#pragma omp parallel for default(none),shared(dx,reduction(+:sum) for(int i = 1; i < numSubdivisions - 1; i++)
{
    double x = A + dx * (float) i;
    double f = Function(x);
    sum += f;
}
sum *= dx;

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       Why Not Do Reduction by Creating Your Own sums Array,
                      one for each Thread, Like This?
float *sums = new float [ omp get num threads() ];
for(int i = 0; i < omp get num threads(); i++)
         sums[i] = 0.;
#pragma omp parallel for private(myPartialSum),shared(sums)
for( int i = 0; i < N; i++)
{
    myPartialSum = ...
    sums[ omp get thread num()] += myPartialSum;
}
float sum = 0.;
for( int i= 0; i < omp_get_num_threads(); i++)
         sum += sums[i];
delete [] sums;
• This seems perfectly reasonable, it works, and it gets rid of the problem of
multiple threads trying to write into the same reduction variable.
• The reason we don't do this is that this method provokes a problem called
False Sharing. We will get to that when we discuss caching.
```