## Sines and Cosines for Animating Computer Graphics

You Know about Sines and Cosines from Math, but They are Very Useful for Animating Computer Graphics

First, We Need to Understand Something about Angles:



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First, We Need to Understand Something about Angles


Fortunately, centuries ago, people developed tables of those $X$ and $Y$ values as functions of $\theta$.

$$
\cos \theta=X
$$

They called the $X$ values cosines and the $Y$ values sines.

$$
\sin \theta=Y
$$

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How People used to Lookup Sines and Cosines - Yuch! Fortunately We Now Have Calculators and Computers


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## Why 2.*PI?

float dang = 2.f*F_PI $/$ (float)numsegs;

We humans commonly measure angles in degrees, but science and computers like to measure them in something else called radians.

There are $360^{\circ}$ in a complete circle.
There are $2 \pi$ radians in a complete circle.
The built-in $\operatorname{cosf()}$ ) and $\operatorname{sinf}()$ functions expect angles to be given in radians.
To convert between the two:
float rad $=$ deg * ( $F_{1}$ PI/180.f);
float deg = rad * (180.f/F_PI);
gIRotatef( ) and gluPerspective( ) are the only two programming

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Circles and Pentagons and Octagons, Oh My!


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> Easy as $\pi:$
> M_PI vs. F_Pl $^{2}$

The math.h include file has a definition of $\pi$ that looks like this:

## \#define M_PI

3.14159265358979323846

Which will work just fine for whatever you need it for.

But, Visual Studio goes a little crazy complaining about mixing doubles (which is what M_PI is in) and floats (which is probably what you use most often). So, your sample code has these lines in it:

$$
\begin{array}{ll}
\text { \#define F_PI } & \left((\text { float })\left(M \_P I\right)\right) \\
\text { \#define F_2_PI } & \left((f l o a t)\left(2 . f \star F_{-P I}\right) \longleftarrow 2 \pi\right. \\
\text { \#define F_PI_2 } & \left(( f l o a t ) \left(F_{-P I / 2 . f))}\right.\right.
\end{array}
$$

I use the $F_{-}$version a lot because it keeps VS quiet. You can use either.

And, there is no reason the $X$ and $Y$ radii need to be the same...


There is also no reason we can't gradually change the radius ...


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## Parametric Linear Interpolation (Blending)

What's this code all about?

```
float t = (float)i / (float)numsegs; // 0.-1.
float newrad = (1.-t)*r0 + t*r1;
```

In computer graphics, we do a lot of linear interpolation between two input values. Here is a good way to do that:

1. Setup a float variable, $\boldsymbol{t}$, such that it ranges from 0 . to 1 .

The line float $t=$ (float) $/$ / (float)numsegs; does this.
2. Step through as many $\boldsymbol{t}$ values as you want interpolation steps.

The line for( int $\mathbf{i}=\mathbf{0} ; \mathbf{i}<=$ numsegs; $\mathbf{i + +}$ ) does this.
3. For each $\boldsymbol{t}$, multiply one input value by (1.-t) and multiply the other input value by $t$ and add them together.
The line float newrad $=(1 .-t)^{\star} \mathbf{r} 0+t^{\star} r 1$; does this.


## We Can Also Use This Same Idea to Arrange Things in a Circle and Linearly Blend Their Colors

```
int numObjects = 9;
float radius = 2.f;
float xc = 3.f;
float yc = 3.f;
int numSegs = 20;
float r = 50.f;
float dang = 2.f*F_PI / (float) ( numObjects - 1 );
float ang = 0.;
for( int i = 0; i < numObjects; i++ )
{
    float x = xc + radius * cosf(ang);
    float y = yc + radius * sinf(ang);
    float t = (float)i / (float)(numObjects-1); // 0.-1.
    float red = t;
    float blue = 1.f - t;
    gIColor3f red, 0., blue );
    Circle( x, y, r, numSegs );
    ang += dang
    }
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```



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## By Understanding what the Sine Function Looks Like, We Can Also Use it to Control Animations Based on Time

In your sample.cpp file, we have some code that looks like this:

```
float Time; // global variable intended to lie between [0.,1.)
const int MS_PER_CYCLE = 10000; // 10000 milliseconds = 10 seconds
// in Animate( )
    int ms = glutGet(GLUT_ELAPSED_TIME);
    ms %=MS_PER_CYCLE;
                            // makes the value of ms between 0 and MS_PER_CYCLE-1
    Time = (float)ms / (float)MS_PER_CYCLE;
        // makes the value of Time between 0. and slightly less than 1.
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> By Understanding what the Sine Function Looks Like, We Can Also Use it to Control Animations Based on Time

The sine function goes from -1 . to +1 ., and does it very smoothly


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\section*{Oscillating Motion}

Let's say you want a block to oscillate back and forth in x :


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```

