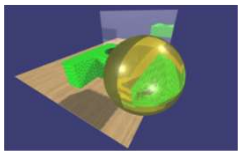
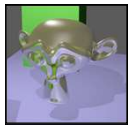
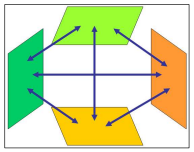




Rendering



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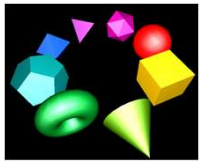
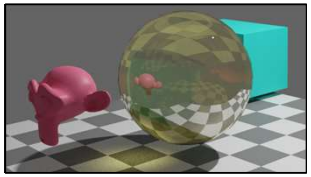
Mike Bailey
mjb@cs.oregonstate.edu





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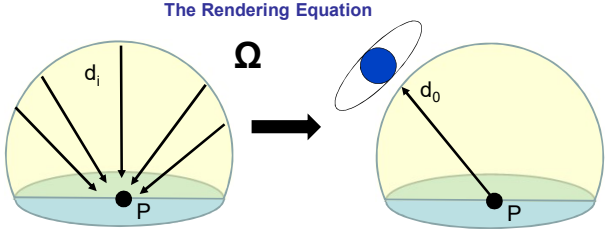
Rendering

Rendering is the process of creating an image of a geometric model.
There are questions you need to ask:

- For what purpose am I doing this?
- How realistic do I need this image to be?
- How much compute time do I have to create this image?
- Do I need to take lighting into account?
- Does the illumination need to be Global or will Local do?
- Do I need to create shadows?
- Do I need to create reflections and refractions?
- How good do the reflections and refractions need to be?

The Rendering Equation



Light arriving at Point P from everywhere

Light departing from Point P in the direction that we are viewing the scene from

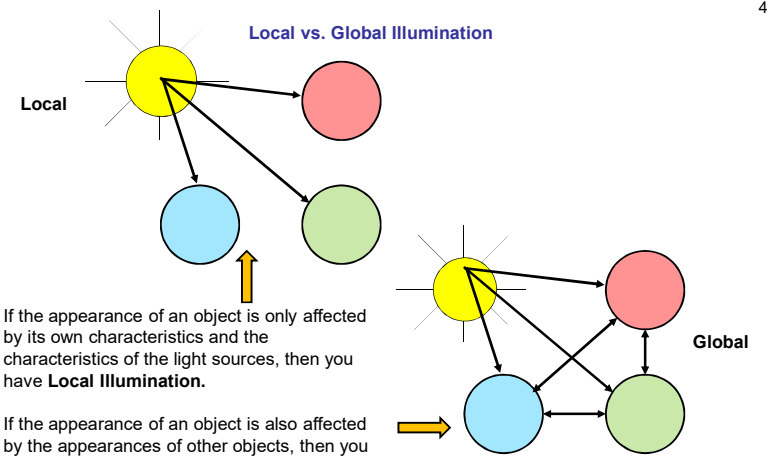
$$B(P, d_0, \lambda) = E(P, d_0, \lambda) + \int_{\Omega} B(P, d_i, \lambda) f(\lambda, d_i, d_0)(d_i \cdot \hat{n}) d\Omega$$

This is the true rendering situation. Essentially, it is an energy balance:

Light Shining from a point P =
Light emitted by that point +
Reflectivity * Σ(Light arriving from all other points)

But, this is time-consuming to solve "exactly".
So, we need to know **how much of an approximation we need**

Local vs. Global Illumination



If the appearance of an object is only affected by its own characteristics and the characteristics of the light sources, then you have **Local Illumination.**

If the appearance of an object is also affected by the appearances of other objects, then you have **Global Illumination.**

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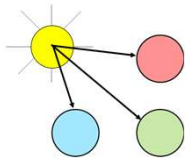
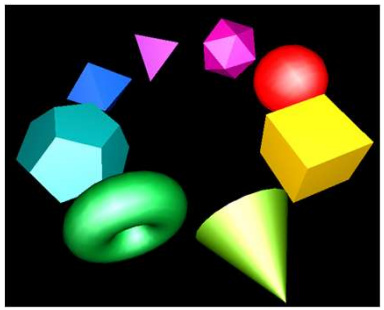
Local Illumination at Work



"If the appearance of an object is only affected by its own characteristics and the characteristics of the light sources, then you have **Local Illumination.**"



OpenGL rendering uses Local Illumination

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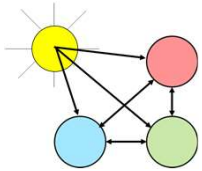
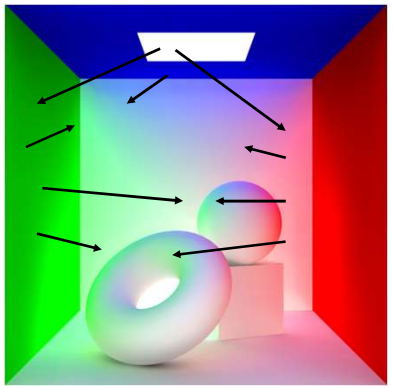
Global Illumination at Work



- The left wall is green.
- The right wall is red.
- The back wall is white.
- The ceiling is blue with a light source in the middle of it.
- The objects sitting on the floor are white.

"If the appearance of an object is also affected by the appearances of other objects, then you have **Global Illumination.**"



http://www.swardson.com/unm/tutorials/mentalRay3/

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Two Directions for the Rendering to Happen

1. Starts at the object, works towards the eye

2. Starts at the eye, works towards the object

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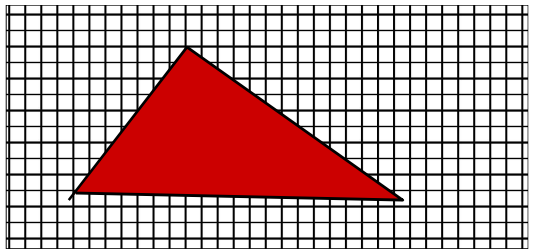
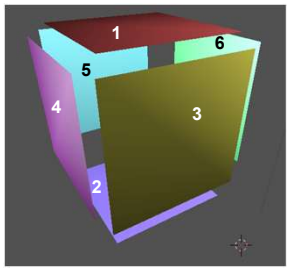
Starts at the Object, Works Towards the Eye

- This is the kind of rendering you get on a graphics card (e.g., OpenGL).
- You have been doing this all along.
- Start with the geometry and project it onto the pixels.



Why do things in front look like they are *really* in front?

Your application might draw this cube's polygons in 1-2-3-4-5-6 order, but 1, 3, and 4 still need to look like they were drawn last:



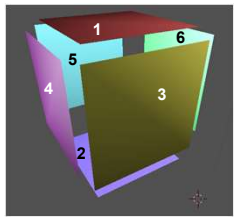
Solution #1: Sort your polygons in 3D by depth and draw them back-to-front.

In this case 1-2-3-4-5-6 becomes 5-6-2-4-1-3.

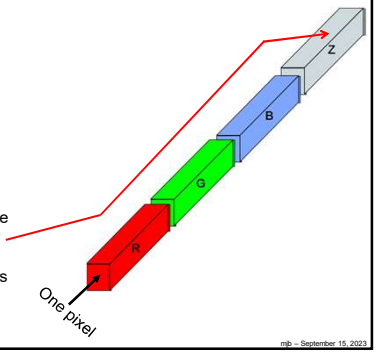
This is called the **Painter's Algorithm**. It sucked to have to do things this way.

Why do things in front look like they are *really* in front?

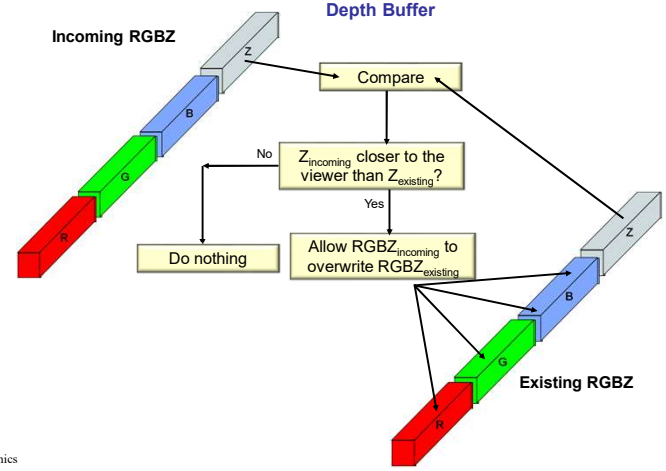
Your application might draw this cube's polygons in 1-2-3-4-5-6 order, but 1, 3, and 4 still need to look like they were drawn last:



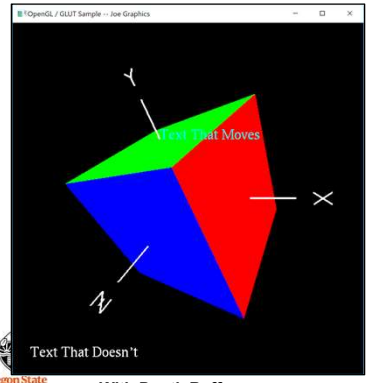
Solution #2: Add an extension to the framebuffer to store the depth of each pixel. This is called a **Depth-buffer** or **Z-buffer.** Only allow pixel stores when the depth of the incoming pixel is closer to the viewer than the pixel that is already there.



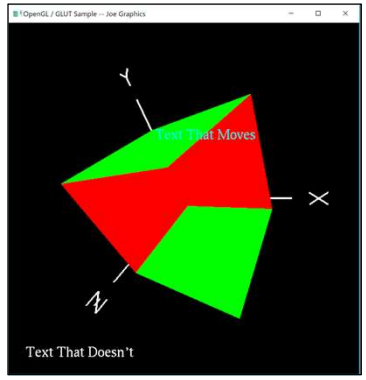
Depth Buffer



Why do things in front look like they are *really* in front?



With Depth Buffer



Without Depth Buffer

Ray-Tracing: Start at the Eye, Work Towards the Objects

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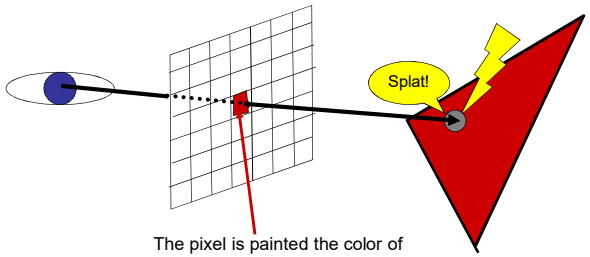

The pixel is painted the color of the nearest object that is hit

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In a Ray-Tracing, each Ray typically hits a lot of Things – You Need to Find All Hits, then Find the Nearest Hit and work from There

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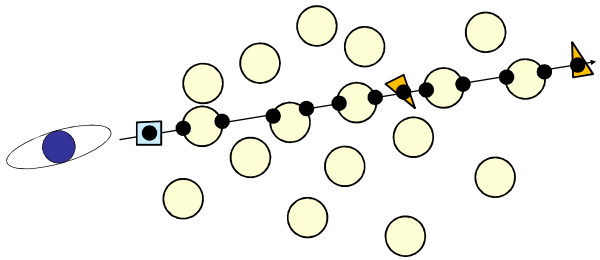

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Ray-Tracing

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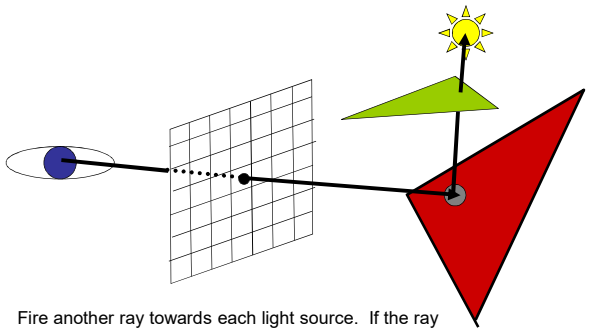
It's also straightforward to see if this point lies in a shadow:



Fire another ray towards each light source. If the ray hits anything, then the point does not receive that light.

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Ray-Tracing

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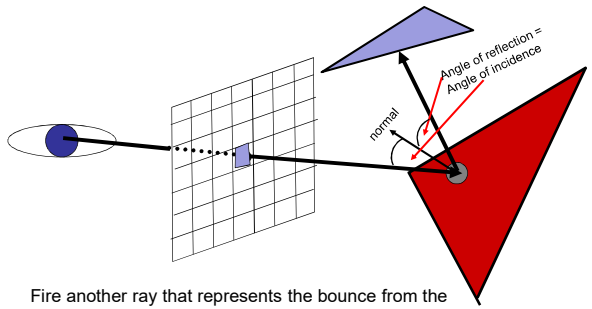
It's also straightforward to handle reflection



Fire another ray that represents the bounce from the reflection. Paint the pixel the color that this ray sees.

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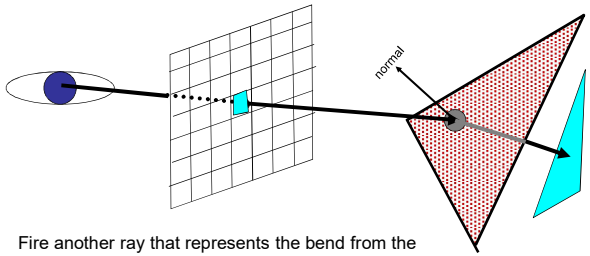
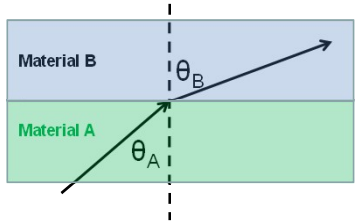
Ray-Tracing

It's also straightforward to handle refraction



Fire another ray that represents the bend from the refraction. Paint the pixel the color that this ray sees.

The Physics of Refraction



Snell's Law of Refraction:

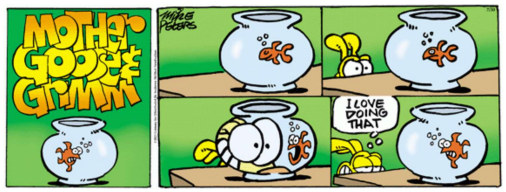
$$\frac{\sin\Theta_B}{\sin\Theta_A} = \frac{\eta_A}{\eta_B}$$

η ⇩

Material	Index of Refraction
Vacuum	1.00000
Air	1.00029
Ice	1.309
Water	1.333
Plexiglass	1.49
Glass	1.60
Diamond	2.42

http://en.wikipedia.org/wiki/Refractive_index

Refraction in Action ☺



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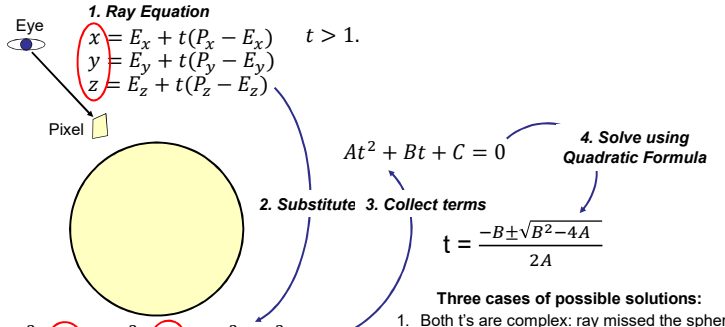
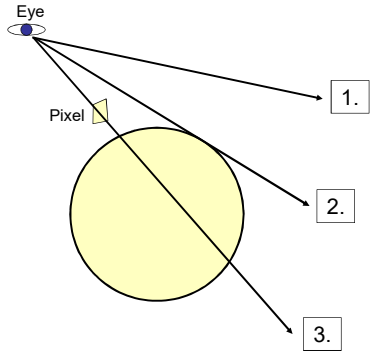
Determining Ray-Shape Intersections



Three cases of possible solutions:

1. Both t's are complex: ray missed the sphere
2. Both t's are real and identical: ray is tangent to the sphere
3. Both t's are real and different: ray goes through the sphere

Determining Ray-Shape Intersections



Three cases of possible solutions:

1. Both t's are complex: ray missed the sphere
2. Both t's are real and identical: ray is tangent to the sphere
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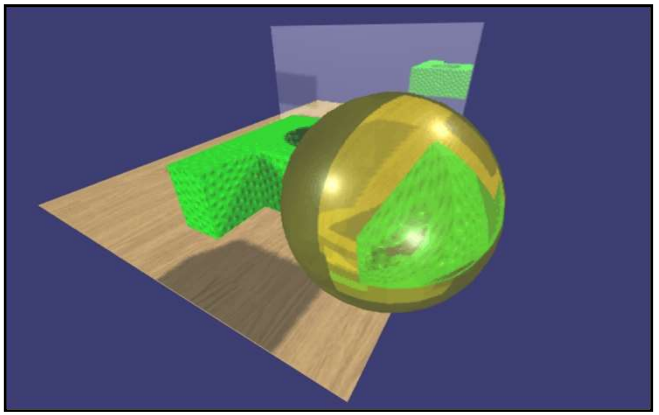
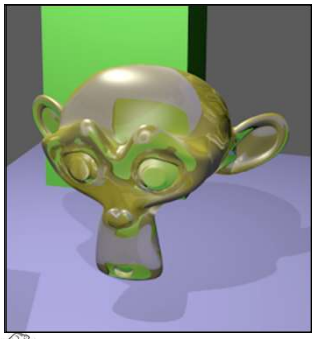
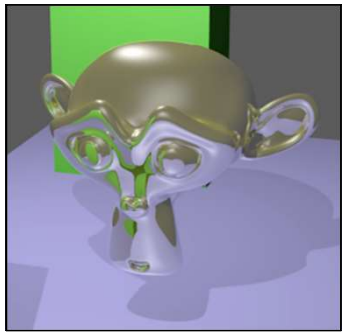
IronCAD Ray-Tracing Example



Blender Ray-Tracing Examples

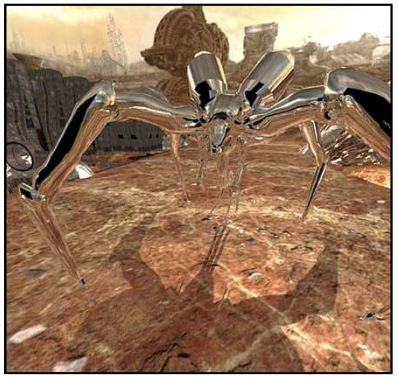


Refraction



Reflection

More Ray-tracing Examples



Quake 4 Ray-Tracing Project

More Ray-Tracing Examples

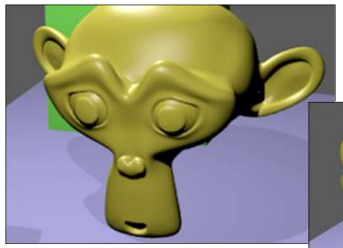
IBM

More Ray-Tracing Examples

Bunkspeed

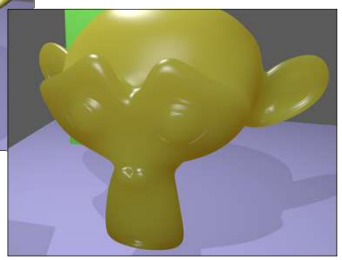
Subsurface Scattering

- Subsurface Scattering mathematically models light bouncing around within an object before coming back out.
- This is a good way to render skin, wax, milk, paraffin, etc.



Original rendering

Subsurface scattering



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The Three Elements of OpenGL Lighting

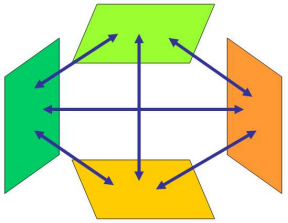
The biggest problem with the Ambient-Diffuse-Specular way of computing lighting is that we are trying to match an appearance, not necessarily follow the laws of physics.

For example, using A-D-S, you can easily create a scene where the amount of light shining from the objects exceeds the amount of light that the light source is supplying!

This brings us to **Physically-Based Rendering (PBR).**

Radiosity

Based on the idea that all surfaces gather light intensity from all other surfaces



The fundamental radiosity equation is an energy balance that says:

"The light energy leaving surface *i* equals the amount of light energy generated by surface *i* plus surface *i*'s reflectivity times the amount of light energy arriving from all other surfaces"

$$B_i A_i = E_i A_i + \rho_i \sum_j B_j A_j F_{j \to i}$$

This is a good approximation to the **Rendering Equation**

The Radiosity Equation

$$B_i A_i = E_i A_i + \rho_i \sum_j B_j A_j F_{j \to i}$$

B_i is the light energy intensity shining from surface element *i*

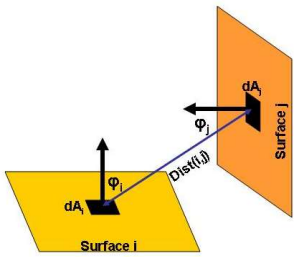
A_i is the area of surface element *i*

E_i is the internally-generated light energy intensity for surface element *i*

ρ_i is surface element *i*'s reflectivity

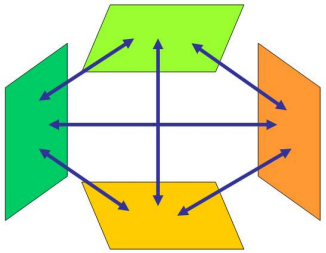
$F_{j \to i}$ is referred to as the **Shape Factor**, and describes what percent of the energy leaving surface element *j* arrives at surface element *i*

The Radiosity Shape Factor



$$F_{j \to i} = \int_{Ai} \int_{A_j} visibility(di, dj) \frac{\cos\Theta_i \cos\Theta_j}{\pi Dist(di, dj)^2} dA_j dA_i$$

I know what you are thinking:
It seems to you that the light just keeps propagating and you never actually get an answer?



To many people, radiosity seems like this:

Use x to get y $y = 3x + 5$

Use y to get x $x = y - 7$

"x produces y, then y produces x, then x produces y, then …"

Not really – it is simply N equations, N unknowns – you solve for the unique solution

$-3x + y = 5$

$x - y = -7$

$x = 1$
$y = 8$

The Radiosity Matrix Equation

$$B_i A_i = E_i A_i + \rho_i \sum_j B_j A_j F_{j \to i} \quad \Longrightarrow \quad B_i A_i - \rho_i \sum_j B_j A_j F_{j \to i} = E_i A_i$$

Expand for each surface element, and re-arrange to **solve for the surface intensities, the *B*'s**:

$$\begin{bmatrix} 1-\rho_1 F_{1\to1} & -\rho_1 F_{1\to2} & \bullet\bullet\bullet & -\rho_1 F_{1\to N} \\ -\rho_2 F_{2\to1} & 1-\rho_2 F_{2\to2} & \bullet\bullet\bullet & -\rho_2 F_{2\to N} \\ \bullet\bullet\bullet & \bullet\bullet\bullet & \bullet\bullet\bullet & \bullet\bullet\bullet \\ -\rho_N F_{N\to1} & -\rho_N F_{N\to2} & \bullet\bullet\bullet & 1-\rho_N F_{N\to N} \end{bmatrix} \begin{Bmatrix} B_1 \\ B_2 \\ \bullet\bullet\bullet \\ B_N \end{Bmatrix} = \begin{Bmatrix} E_1 \\ E_2 \\ \bullet\bullet\bullet \\ E_N \end{Bmatrix}$$

This is a lot of equations!

Radiosity Examples

Cornell University

Cornell University

Radiosity Examples

AR Toolkit

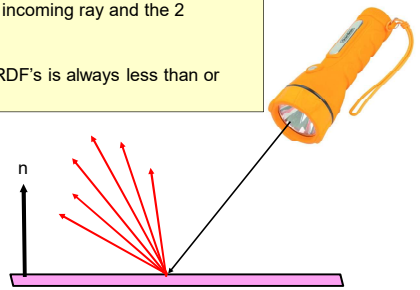
Autodesk

Path Tracing: When light hits a surface, it bounces in particular ways depending on the angle and the material

This distribution of bounced light rays is called the **Bidirectional Reflectance Distribution Function**, or **BRDF**.

For a given material, the BRDF behavior of a light ray is a function of 4 variables: the 2 spherical coordinates of the incoming ray and the 2 spherical coordinates of the outgoing ray.

The outgoing light energy in the outgoing BRDF's is always less than or equal to the amount of light that shines in.



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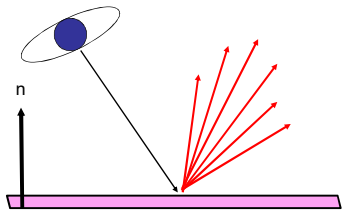
Usually it is easier to trace from the eye



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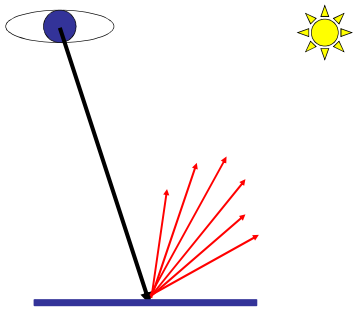
Path Tracing

Somewhat like ray-tracing, somewhat like radiosity where light can bounce around the scene but this has more sophisticated effects.



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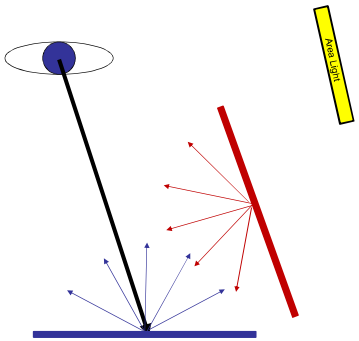
Path Tracing



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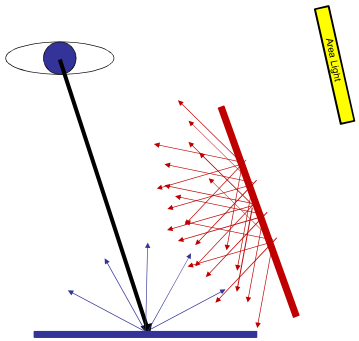
Path Tracing



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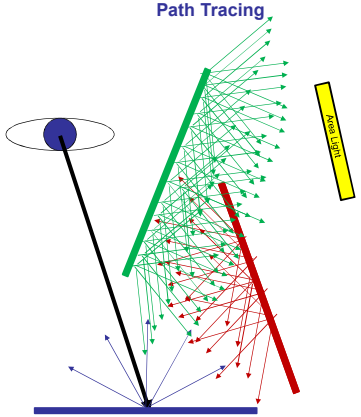
Path Tracing



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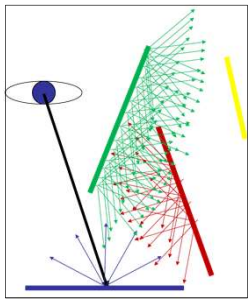
Path Tracing



Clearly this is capable of spawning an infinite number of rays. How do we handle this?

Monte Carlo simulation to the rescue!

Each time a ray hits a surface, use the equation at that point. Continue until:

1. Nothing is hit
2. A light is hit
3. Some maximum number of bounces are found

$$LightGathered = \frac{\sum_0^{N-1} ResultOfRaysCastInRandomDirection}{N}$$

Recurse by applying this equation for all ray hits (yikes!)

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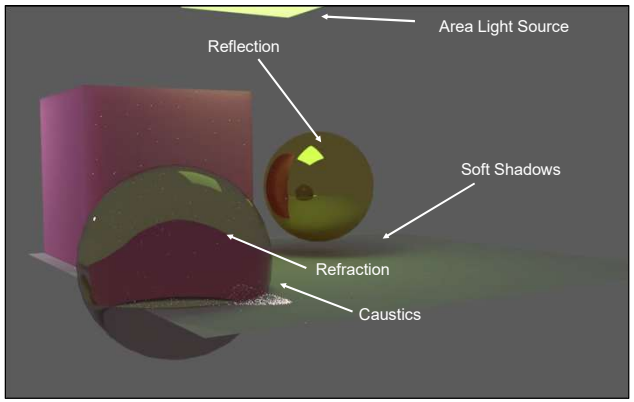
Physically-Based Rendering using the Blender *Cycles* Renderer



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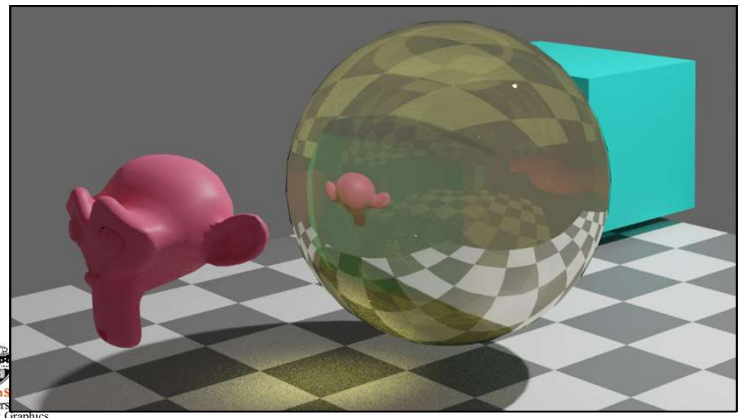
Physically-Based Rendering using the Blender *Cycles* Renderer



Another Physically-Based Rendering Example

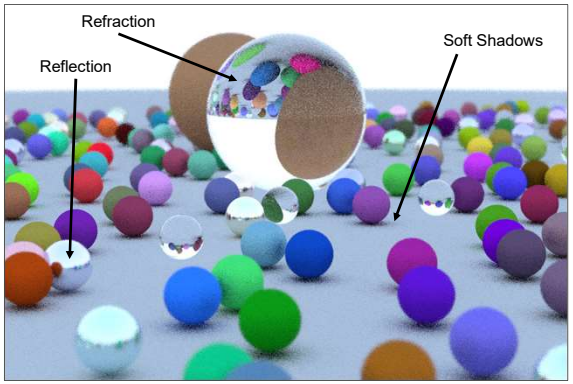
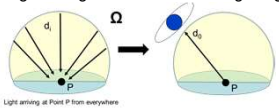


Image by Josiah Blaisdell

Something New: Neural Radiance Fields -- NeRFs

What if you want to know what an object looks like no matter where other light is coming from and no matter where you view it from? You could go through the whole rendering thing from every viewing angle…



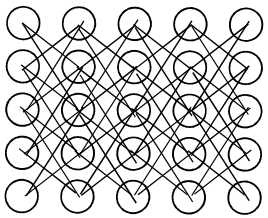
…but that would be time consuming and would preclude any sort of real-time scene manipulation.

In the NeRFs technique, you precompute, for every incoming light direction how much of that ends up in every outgoing viewing direction. Then, when interacting with the scene, you don't need to do any actual "rendering". You just track the radiance outputs from an object and use those as inputs to other objects and use those precomputed values to see what comes out of that object.

How can we lookup that information quickly?

NeRFs: Machine Learning to the Rescue!

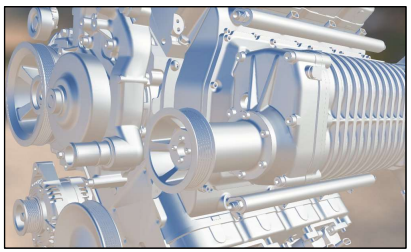
For each object, you train a neural network …

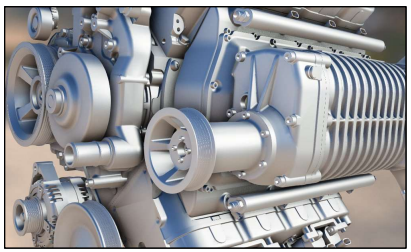


…on the pre-rendered data so that a radiance input to that object can quickly be turned into a radiance output from that object

This is very new technique, but something worth keeping an eye on!

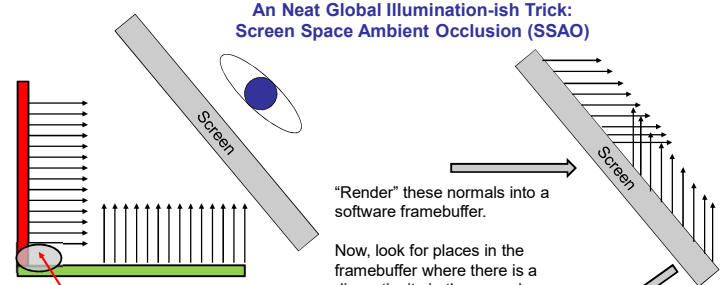
An Neat Global Illumination-ish Trick: Screen Space Ambient Occlusion (SSAO)





Kitware

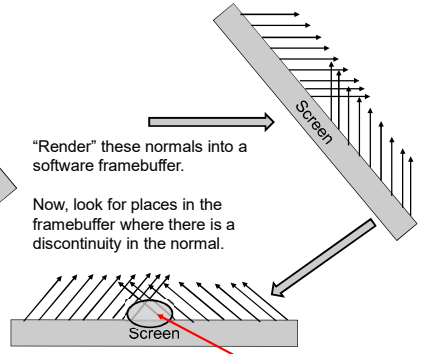
An Neat Global Illumination-ish Trick: Screen Space Ambient Occlusion (SSAO)



This part of the scene should be darker because it is harder for ambient light to get down between objects.

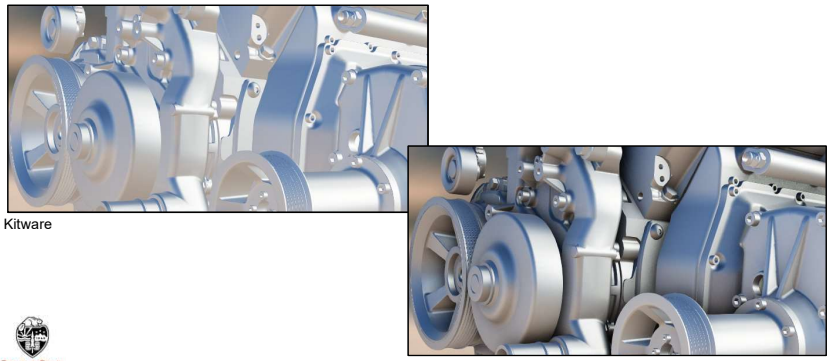
"Render" these normals into a software framebuffer.

Now, look for places in the framebuffer where there is a discontinuity in the normal.



Make that part of the scene darker.

An Neat Global Illumination-ish Trick: Screen Space Ambient Occlusion (SSAO)



Kitware